## Birzeit University <br> Department of Electrical and Computer Engineering Faculty of Engineering and Technology

ENCS 539: Information Retrieval and Web Search, Quiz , January 13, 2018
Student Name: $\qquad$ Sample Solution Student Number: $\qquad$

We have 4 web pages with their connections as shown on the figure below.
Assume that the initial values for Hub, Authority and PageRank for all pages are 1.
That is $a_{i}(0)=1, h_{i}(0)=1, P R_{i}(0)=1$ for all $i \in=\{1, \ldots 4\}$.
Fill the table below with the values of $a, h, P R$ for 3 iterations at most.


| Page $\rightarrow$ <br> a/h/PR $\downarrow$ | $\begin{gathered} A: h(A)=a(B)+a(C) \\ a(A)=h(C) \end{gathered}$ | $\begin{aligned} B: h(B) & =a(C) \\ a(B) & =h(A) \end{aligned}$ | $\begin{aligned} & \text { C: } \mathrm{h}(\mathrm{C})=\mathrm{a}(\mathrm{~A}) \\ & \mathrm{a}(\mathrm{C})=\mathrm{h}(\mathrm{~A})+\mathrm{h}(\mathrm{~B})+\mathrm{h}(\mathrm{D}) \end{aligned}$ | $\begin{gathered} \text { D: } \mathrm{h}(\mathrm{~A})=\mathrm{a}(\mathrm{C}) \\ \mathrm{a}(\mathrm{D})=0 \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: |
| a(0) | 1 | 1 | 1 | 1 |
| h(0) | 1 | 1 | 1 | 1 |
| a(1) | 1(1) | 1(1) | 3(3) | O(0) |
| h(1) | 2(4) | 1(3) | 1(1) | 1(3) |
| a(2) | 1(1) | 2(4) | $2+1+1=4(10)$ | O(0) |
| h(2) | 4(14) | 3(10) | 1(1) | 3(10) |
| a(3) | 4(1) | 4(14) | $1+3+3=7(34)$ | O(0) |
| h(3) | 2+4=6 (38) | 4(24) | 1(1) | 4(34) |
| PR(0) | 1: $\operatorname{PR}(\mathrm{A})=\mathrm{PR}(\mathrm{C})$ | 1: $\operatorname{PR}(\mathrm{B})=0.5 * \operatorname{PR}(\mathrm{~A})$ | $\begin{aligned} & \text { 1: } \mathrm{PR}(\mathrm{C})=0.5^{*} \mathrm{PR}(\mathrm{~A})+ \\ & \mathrm{PR}(\mathrm{~B})+\mathrm{PR}(\mathrm{D}) \end{aligned}$ | 1: PR(D)=0 |
| PR (1) | 1 | 0.5 | $0.5+1+1=2.5$ | 0 |
| PR (2) | 2.5 | 0.5 | $0.5+0.5+0=1$ | 0 |
| PR (3) | 1 | 1.25 | $1.25+0.5+0=1.75$ | 0 |

Note that for the Authority and Hub we provided two cases: one is the correct where we use the previous stage values (to compute $\mathrm{h}(\mathrm{i})$ we use $\mathrm{a}(\mathrm{i}-1)$ and to compute $\mathrm{a}(\mathrm{i})$ we use $\mathrm{h}(\mathrm{i}-1)$ ). The less correct -in ()-is when we the above in the table values of the other parameter: for a's use preceding h in the table and for h 's use preceding a's in the table. This doesn't change the a's for the first iteration but changes later iterations. The order of computing (a then h or h then a becomes relevant). You use the first (correct one) if asked to compute a's and h's.

Also when computing PageRank, if teleporting with $\mathrm{X} \%$ is used then each node gets an extra ( $\mathrm{X} / \mathrm{N}$ )\% plus what it gets from the remaining part of the PR of the source nodes of incoming links. $N$ is the total number of nodes in the graph. In our example, if we teleport with $40 \%$ then each node gets $10 \%$ from the teleport plus the proportion it gets from incoming links.

